

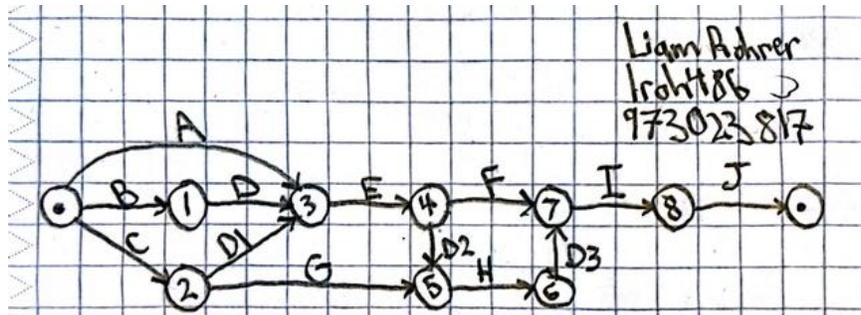
### STATS 255 Assignment 3

1.

a.

| TASK | PREDECESSORS |
|------|--------------|
| A    | -            |
| B    | -            |
| C    | -            |
| D    | B            |
| E    | A, C, D      |
| F    | E            |
| G    | C            |
| H    | E, G         |
| I    | H, F         |
| J    | I            |

b.



c.

| activity | from | to | a  | m  | b  | EST    | EFT    | LST    | LFT    | slack  | expected task time | std deviation | variance |
|----------|------|----|----|----|----|--------|--------|--------|--------|--------|--------------------|---------------|----------|
| A        | .    | 3  | 3  | 4  | 5  | 0.000  | 4.000  | 9.333  | 13.333 | 9.333  | 4.000              | 0.333         | 0.111    |
| B        | .    | 1  | 4  | 5  | 9  | 0.000  | 5.500  | 0.000  | 5.500  | 0.000  | 5.500              | 0.833         | 0.694    |
| C        | .    | 2  | 1  | 1  | 2  | 0.000  | 1.167  | 12.167 | 13.333 | 12.167 | 1.167              | 0.167         | 0.028    |
| D        | 1    | 3  | 6  | 8  | 9  | 5.500  | 13.333 | 5.500  | 13.333 | 0.000  | 7.833              | 0.500         | 0.250    |
| E        | 3    | 4  | 3  | 4  | 6  | 13.333 | 17.500 | 13.333 | 17.500 | 0.000  | 4.167              | 0.500         | 0.250    |
| F        | 4    | 7  | 10 | 12 | 17 | 17.500 | 30.000 | 17.500 | 30.000 | 0.000  | 12.500             | 1.167         | 1.361    |
| G        | 2    | 5  | 5  | 7  | 9  | 1.167  | 8.167  | 19.833 | 26.833 | 18.667 | 7.000              | 0.667         | 0.444    |
| H        | 5    | 6  | 2  | 3  | 5  | 17.500 | 20.667 | 26.833 | 30.000 | 9.333  | 3.167              | 0.500         | 0.250    |
| I        | 7    | 8  | 3  | 4  | 5  | 30.000 | 34.000 | 30.000 | 34.000 | 0.000  | 4.000              | 0.333         | 0.111    |
| J        | 8    | .  | 2  | 4  | 5  | 34.000 | 37.833 | 34.000 | 37.833 | 0.000  | 3.833              | 0.500         | 0.250    |
| D1       | 2    | 3  | 0  | 0  | 0  | 1.167  | 1.167  | 13.333 | 13.333 | 12.167 | 0.000              | 0.000         | 0.000    |
| D2       | 4    | 5  | 0  | 0  | 0  | 17.500 | 17.500 | 26.833 | 26.833 | 9.333  | 0.000              | 0.000         | 0.000    |
| D3       | 6    | 7  | 0  | 0  | 0  | 20.667 | 20.667 | 30.000 | 30.000 | 9.333  | 0.000              | 0.000         | 0.000    |

expected project completion time 37.833  
 variance of project completion time 2.917  
 std deviation of project completion time 1.708

probability to complete the project in a time of at most 30 time units is 2.251E-06  
 to complete project with a certainty of alpha 0.7 target completion time is 38.7289164

| completion time | completion probability |
|-----------------|------------------------|
| 41.18           | 0.975                  |
| 40.64           | 0.95                   |
| 40.02           | 0.90                   |
| 39.60           | 0.85                   |
| 38.99           | 0.75                   |
| 38.49           | 0.65                   |
| 37.83           | 0.50                   |
| 37.18           | 0.35                   |
| 36.68           | 0.25                   |
| 36.06           | 0.15                   |
| 35.64           | 0.10                   |
| 35.02           | 0.05                   |

- d. Critical path: B → D → E → F → I → J
- e. They should allow 41.806 days for the project to be 99% sure it will be done in time.
- f. The director should not be worried about a 12 day increase for this activity. The costume design and making step has a slack time of 18.667 days, which means that the activity duration can increase up to this amount before the overall project completion time is affected.

2.

a.

|    | AM           | AN    | AO | AP           | AQ | AR | AS | AT                            | AU          |
|----|--------------|-------|----|--------------|----|----|----|-------------------------------|-------------|
| 1  |              |       |    |              |    |    |    |                               | Liam Rohrer |
| 2  |              |       |    |              |    |    |    |                               | Iroh486     |
| 3  |              |       |    |              |    |    |    |                               | 973023817   |
| 4  | Activity:    | A     | B  | C            | D  | E  | F  |                               |             |
| 5  | Reduction:   | 0     | 2  | 4            | 0  | 1  | 0  |                               |             |
| 6  |              |       |    |              |    |    |    |                               |             |
| 7  | MIN:         | 1     | 2  | 3            | 4  | 5  | 6  | =SUMPRODUCT(AN5:AS5, AN7:AS7) |             |
| 8  | Constraints: | =AN5  | <= | 6            |    |    |    |                               |             |
| 9  |              | =AO5  | <= | 5            |    |    |    |                               |             |
| 10 |              | =AP5  | <= | 4            |    |    |    |                               |             |
| 11 |              | =AQ5  | <= | 3            |    |    |    |                               |             |
| 12 |              | =AR5  | <= | 2            |    |    |    |                               |             |
| 13 |              | =AS5  | <= | 1            |    |    |    |                               |             |
| 14 | Node 0       | =AN26 | =  | 0            |    |    |    |                               |             |
| 15 | Node 1       | =AO26 | >= | =AN17        |    |    |    |                               |             |
| 16 | Node 1       | =AO26 | >= | =AN14+15-AN5 |    |    |    |                               |             |
| 17 | Node 2       | =AP26 | >= | =AN14+17-AO5 |    |    |    |                               |             |
| 18 | Node 3       | =AQ26 | >= | =AN14+19-AP5 |    |    |    |                               |             |
| 19 | Node 4       | =AR26 | >= | =AN17        |    |    |    |                               |             |
| 20 | Node 4       | =AR26 | >= | =AN18+7-AR5  |    |    |    |                               |             |
| 21 | Node 5       | =AS26 | >= | =AN15+9-AQ5  |    |    |    |                               |             |
| 22 | Node 5       | =AS26 | >= | =AN19+3-AS5  |    |    |    |                               |             |
| 23 | Node 5       | =AS26 | <= | 24           |    |    |    |                               |             |
| 24 |              |       |    |              |    |    |    |                               |             |
| 25 | Node:        | 0     | 1  | 2            | 3  | 4  | 5  |                               |             |
| 26 | EST:         | 0     | 15 | 15           | 15 | 21 | 24 |                               |             |

| A                    | B    | C              | D           | E | F | G | H | I  |             |          |                |            |                    |             |       |
|----------------------|------|----------------|-------------|---|---|---|---|----|-------------|----------|----------------|------------|--------------------|-------------|-------|
| Objective Cell (Min) |      |                |             |   |   |   |   | 35 | Constraints |          |                |            |                    |             |       |
| Cell                 | Name | Original Value | Final Value |   |   |   |   |    | 36          | Cell     | Name           | Cell Value | Formula            | Status      | Slack |
| \$AT\$7              | MIN: | 21             | 21          |   |   |   |   |    | 37          | \$AN\$14 | Node 0 A       | 0          | \$AN\$14=\$AP\$14  | Binding     | 0     |
|                      |      |                |             |   |   |   |   |    | 38          | \$AN\$15 | Node 1 A       | 15         | \$AN\$15>=\$AP\$15 | Binding     | 0     |
|                      |      |                |             |   |   |   |   |    | 39          | \$AN\$16 | Node 1 A       | 15         | \$AN\$16>=\$AP\$16 | Binding     | 0     |
|                      |      |                |             |   |   |   |   |    | 40          | \$AN\$17 | Node 2 A       | 15         | \$AN\$17>=\$AP\$17 | Binding     | 0     |
|                      |      |                |             |   |   |   |   |    | 41          | \$AN\$18 | Node 3 A       | 15         | \$AN\$18>=\$AP\$18 | Binding     | 0     |
|                      |      |                |             |   |   |   |   |    | 42          | \$AN\$19 | Node 4 A       | 21         | \$AN\$19>=\$AP\$19 | Not Binding | 6     |
|                      |      |                |             |   |   |   |   |    | 43          | \$AN\$20 | Node 4 A       | 21         | \$AN\$20>=\$AP\$20 | Binding     | 0     |
|                      |      |                |             |   |   |   |   |    | 44          | \$AN\$21 | Node 5 A       | 24         | \$AN\$21>=\$AP\$21 | Binding     | 0     |
|                      |      |                |             |   |   |   |   |    | 45          | \$AN\$22 | Node 5 A       | 24         | \$AN\$22>=\$AP\$22 | Binding     | 0     |
|                      |      |                |             |   |   |   |   |    | 46          | \$AN\$23 | Node 5 A       | 24         | \$AN\$23<=\$AP\$23 | Binding     | 0     |
|                      |      |                |             |   |   |   |   |    | 47          | \$AN\$8  | Constraints: A | 0          | \$AN\$8<=\$AP\$8   | Not Binding | 6     |
|                      |      |                |             |   |   |   |   |    | 48          | \$AN\$9  | C A            | 2          | \$AN\$9<=\$AP\$9   | Not Binding | 3     |
|                      |      |                |             |   |   |   |   |    | 49          | \$AN\$10 | D A            | 4          | \$AN\$10<=\$AP\$10 | Binding     | 0     |
|                      |      |                |             |   |   |   |   |    | 50          | \$AN\$11 | E A            | 0          | \$AN\$11<=\$AP\$11 | Not Binding | 3     |
|                      |      |                |             |   |   |   |   |    | 51          | \$AN\$12 | F A            | 1          | \$AN\$12<=\$AP\$12 | Not Binding | 1     |
|                      |      |                |             |   |   |   |   |    | 52          | \$AN\$13 | A              | 0          | \$AN\$13<=\$AP\$13 | Not Binding | 1     |

| Cell     | Name         | Original Value | Final Value | Integer |
|----------|--------------|----------------|-------------|---------|
| \$AN\$5  | Reduction: A | 0              | 0           | Contin  |
| \$AO\$5  | Reduction: B | 2              | 2           | Contin  |
| \$AP\$5  | Reduction: C | 4              | 4           | Contin  |
| \$AQ\$5  | Reduction: D | 0              | 0           | Contin  |
| \$AR\$5  | Reduction: E | 1              | 1           | Contin  |
| \$AS\$5  | Reduction: F | 0              | 0           | Contin  |
| \$AN\$26 | EST: A       | 0              | 0           | Contin  |
| \$AO\$26 | EST: <=      | 15             | 15          | Contin  |
| \$AP\$26 | EST: C       | 15             | 15          | Contin  |
| \$AQ\$26 | EST: D       | 15             | 15          | Contin  |
| \$AR\$26 | EST: E       | 21             | 21          | Contin  |
| \$AS\$26 | EST: F       | 24             | 24          | Contin  |

b. Tasks to be crashed: B by 2 days, C by 4 days, and E by 1 day

c.

| Project Duration (days) | Total Crash Cost (\$) | Marginal Crash Cost (\$/day) |
|-------------------------|-----------------------|------------------------------|
| 29                      | 0                     | N/A                          |
| 28                      | 3                     | 3                            |
| 27                      | 6                     | 3                            |
| 26                      | 9                     | 3                            |
| 25                      | 14                    | 5                            |
| 24                      | 21                    | 7                            |
| 23                      | 29                    | 8                            |

d. Marginal costs tend to increase as crash time increases.

3.

a. A deterministic EOQ is the most appropriate inventory model for this situation.

$$D = 25$$

$$C = 3$$

$$K = 15$$

$$L = 3$$

$$H = 0.03$$

b. (shown below)

c. (shown below)

b.  $Q^* = \sqrt{\frac{2DK}{H}} = \sqrt{\frac{2(25)(15)}{0.03}} = 158.11 \rightarrow 158 \text{ drinks}$

c. (Holding cost is fixed, so  $Q^*$  doesn't change)

$(Q=150) T_1 = \frac{15(25)}{150} + 3(25) + \frac{150}{2}(0.03) = 2.5 + 75 + 2.25 = 79.75$

$(Q=158) T_2 = \frac{15(25)}{158} + 2.7(25) + \frac{158}{2}(0.03) = 2.37 + 67.5 + 2.37 = 72.04$

$(Q=201) T_3 = \frac{15(25)}{201} + 2.6(25) + \frac{201}{2}(0.03) = 1.87 + 65 + 3.02 = 69.89$

We achieve the lowest cost by ordering 201 drinks at a cost of \$2.60 a drink.

d. A deterministic POQ is the most appropriate inventory model for this situation.

e. (shown below)

f. (shown below)

g. (shown below)

e.  $D=25$   
 $C=2.5$   
 $L=6$   
 $K=50$   
 $H=0.03$   
 $P=45$

$Q^* = \sqrt{\frac{2DK}{(P-D)H}} = \sqrt{\frac{2(25)(50)}{(45-25)0.03}} = 433.01 \rightarrow 433 \text{ drinks}$

f.

g.  $R = D * L = 25 * 6 = 150$  ( $17.32 - 9.62 = 7.7 \rightarrow 7.7 > 6$   
 The re-order point occurs after the production run meaning we have a short lead time.)